# A CRITICAL POPULATION THRESHOLD FOR CONTACT-INDUCED SIMPLIFICATION 

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Learning biases have long been theorized to play a causal role in the cultural evolution of linguistic systems. In particular, existing literature suggests that the difficulty encountered by second-language (L2) learners in acquiring complex linguistic features may contribute to the loss of those features from the target language in situations of language contact (Bentz \& Winter, 2013; Berdicevskis \& Semenuks, 2022; Lupyan \& Dale, 2010; Sinnemäki \& Di Garbo, 2018; Trudgill, 2011; Walkden \& Breitbarth, 2019; Weerman, 1993; also see Jansson, Parkvall, \& Strimling, 2015 on modelling creolization). Against the backdrop of this body of research, it is reasonable to expect that the population fraction of L2 learners may act as a bifurcation parameter: if sufficiently many L2 learners are present in a speech community, the loss of L2-difficult features may be permanent. Without an explicit model combining population and learning dynamics, however, it is impossible to say where the critical value of such a putative bifurcation parameter might lie.

We propose such a model by extending the variational learner (Yang, 2002) to cover L2 as well as L1 acquisition. For L2 (but not L1) learners, the extended model includes a learning bias that works against the successful (native-like) acquisition of the L2-difficult variant. The asymptotic dynamics of this extended learning model can be studied just like those of the ordinary linear reward-penalty learning scheme (Bush \& Mosteller, 1955) that underlies the variational learner. In particular, we show that an L2 learner's expected probability of employing an L2-difficult grammar $G_{1}$ over its easier-to-acquire competitor $G_{2}$ tends to a definite value as learning iteration tends to infinity.

Taking the usual infinite learner limit (cf. Yang, 2000) then yields a deterministic dynamical system that describes the evolution of a mixed population of L1 and L 2 speakers. This system has three parameters: $\sigma$, the fraction of L 2 speakers in the population; $D$, the learning-theoretic strength of the L2-difficulty of $G_{1}$; and $\alpha$, the fitness ratio (Kauhanen \& Walkden, 2018) of the two grammars.

We show analytically that this system always has exactly one stable equilibrium. The system's dynamics are, however, separated into two phases: in one
phase, the stable equilibrium satisfies $p>0$ and $q>0$, where $p$ and $q$ stand for the probability of the L2-difficult grammar $G_{1}$ in the L1 and L2 populations, respectively. In other words, the L2-difficult grammar is retained in each population at some non-zero (and possibly high) frequency. In the second phase, however, the attractor is the origin $(p, q)=(0,0)$, meaning that the L2-difficult grammar is wiped out from both populations, including the L1 speaker population which itself is not subject to the learning bias (but feels its effects through interactions with the L 2 population). This bifurcation occurs as $\sigma$ crosses the critical value

$$
\begin{equation*}
\sigma_{\mathrm{crit}}=\frac{(\alpha-1)(D+1)}{\alpha D} \tag{1}
\end{equation*}
$$

that is, fractions of L2 speakers $\sigma>\sigma_{\text {crit }}$ exhibit simplification dynamics (Fig. 1).
To provide some empirical support for the model, we estimate the parameters $\sigma$ and $\alpha$ from demographic and corpus data, and provide reasonable orders of magnitude for the learning bias $D$, for two historical developments: the loss of verbal inflection in Afrikaans (Trudgill, 2011) and the partial loss of null subjects in Afro-Peruvian Spanish (Sessarego \& Gutiérrez-Rexach, 2018). Empirically, the simplification process in Afrikaans went to completion, whereas in Afro-Peruvian Spanish null subjects retain a partial status. These facts are predicted by the model, in the sense that $\sigma>\sigma_{\text {crit }}$ in the former case but not in the latter.


Figure 1. Stable equilibrium $(p, q)$ of the mixed speech community (top row: probability of $G_{1}$ in L1 speakers; bottom row: L2 speakers). Full simplification occurs above the bifurcation threshold $\sigma_{\text {crit }}$ (equation 1), depicted as the dashed white curve.

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